DO NOT OPEN THIS TEST BOOKLET UNTIL YOU ARE TOLD TO DO SO

T.B.C. : ADN-S-SND

Serial No.

1360053



Test Booklet Series



TEST BOOKLET MATHEMATICS

Time Allowed: Two Hours and Thirty Minutes

Maximum Marks: 300

INSTRUCTIONS

- IMMEDIATELY AFTER THE COMMENCEMENT OF THE EXAMINATION, YOU SHOULD CHECK THAT 1. THIS TEST BOOKLET DOES NOT HAVE ANY UNPRINTED OR TORN OR MISSING PAGES OR ITEMS. ETC. IF SO, GET IT REPLACED BY A COMPLETE TEST BOOKLET.
- Please note that it is the candidate's responsibility to encode and fill in the Roll Number and Test 2. Booklet Series Code A, B, C or D carefully and without any omission or discrepancy at the appropriate places in the OMR Answer Sheet. Any omission/discrepancy will render the Answer Sheet liable for rejection.
- You have to enter your Roll Number on the 3. Test Booklet in the Box provided alongside.

DO NOT write anything else on the Test Booklet.

- This Test Booklet contains 120 items (questions). Each item is printed both in Hindi and English. 4. Each item comprises four responses (answers). You will select the response which you want to mark on the Answer Sheet. In case you feel that there is more than one correct response, mark the response which you consider the best. In any case, choose ONLY ONE response for each item.
- You have to mark all your responses ONLY on the separate Answer Sheet provided. See directions 5. in the Answer Sheet.

All items carry equal marks. 6.

- Before you proceed to mark in the Answer Sheet the response to various items in the Test Booklet, 7. you have to fill in some particulars in the Answer Sheet as per instructions sent to you with your Admission Certificate.
- After you have completed filling in all your responses on the Answer Sheet and the examination has concluded, you should hand over to the Invigilator only the Answer Sheet. You are permitted to take away with you the Test Booklet.
- Sheets for rough work are appended in the Test Booklet at the end. 9.
- Penalty for wrong answers: 10.

THERE WILL BE PENALTY FOR WRONG ANSWERS MARKED BY A CANDIDATE IN THE OBJECTIVE TYPE QUESTION PAPERS.

- There are four alternatives for the answer to every question. For each question for which a wrong answer has been given by the candidate, one-third (0-33) of the marks assigned to that question will be deducted as penalty.
- If a candidate gives more than one answer, it will be treated as a wrong answer even if one of the given (ii) answers happens to be correct and there will be same penalty as above to that question.
- If a question is left blank, i.e., no answer is given by the candidate, there will be no penalty for that (iii) question.

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ध्यान दें : अनुदेशों का हिन्दी रूपान्तर इस पुस्तिका के पिछले पृष्ठ पर छपा है ।

(1-A)ADN-S-SND

- 1. Let S be a set of all distinct numbers of the form $\frac{p}{q}$, where p, $q \in \{1, 2, 3, 4, 5, 6\}$. What is the cardinality of the set S?
 - (a) 21
 - (b) 23
 - (c) 32
 - (d) 36
- 2. If c > 0 and 4a + c < 2b, then ax² bx + c = 0 has a root in which one of the following intervals?
 - (a) (0, 2)
 - (b) (2, 3)
 - (c) (3, 4)
 - (d) (-2,0)
- 3. If $A = \{x \in \mathbb{R} : x^2 + 6x 7 < 0\}$ and $B = \{x \in \mathbb{R} : x^2 + 9x + 14 > 0\}$, then which of the following is/are correct?
 - 1. $A \cap B = \{x \in \mathbb{R} : -2 < x < 1\}$
 - 2. $A \setminus B = \{x \in \mathbb{R} : -7 < x < -2\}$

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- (e) Both 1 and 2
- (d) Neither 1 nor 2
- 4. If A is a square matrix of order 3 and det A = 5, then what is det [(2A)⁻¹] equal to?
 - (a) 1/10
 - (b) 2/5
 - (c) 8/5
 - (d) 1/40

- 5. What is $\omega^{100} + \omega^{200} + \omega^{300}$ equal to, where ω is the cube root of unity?
 - (a) 1
 - (b) 3w
 - (c) 3ω²
 - (d) 0
- 6. If $\operatorname{Re}\left(\frac{z-1}{z+1}\right) = 0$, where z = x + iy is a complex number, then which one of the following is correct?
 - (a) z = 1 + i
 - (b) | z | = 2
 - (c) z = 1 i
 - (d) | z | = 1
- 7. What is $\begin{bmatrix} x & y & z \end{bmatrix} \begin{bmatrix} a & h & g \\ h & b & f \\ g & f & c \end{bmatrix}$ equal to?
 - (a) $[ax + hy + gz \quad h + b + f \quad g + f + c]$

 - (c) $\begin{bmatrix} ax + hy + gz \\ hx + by + fz \\ gx + fy + cz \end{bmatrix}$
 - (d) $[ax + hy + gz \quad hx + by + fz \quad gx + fy + cz]$

- 8. Out of 15 points in a plane, n points are in the same straight line. 445 triangles can be formed by joining these points. What is the value of n?
 - (a) 3
 - (b) 4
 - (c) 5
 - (d) 6
- 9. If $z = \left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^{107} + \left(\frac{\sqrt{3}}{2} \frac{i}{2}\right)^{107}$, then what is the imaginary part of z equal to?
 - (a) 0
 - (b) $\frac{1}{2}$
 - (e) $\frac{\sqrt{3}}{2}$
 - (d) 1
- 10. If both the roots of the equation $x^2-2kx+k^2-4=0 \ \text{lie between}-3 \ \text{and} \ 5,$ then which one of the following is correct?
 - (a) -2 < k < 2
 - (b) −5 < k < 3
 - (c) -3 < k < 5
 - (d) -1 < k < 3
- 11. What is the number of distinct solutions of the equation $z^2 + |z| = 0$ (where z is a complex number)?
 - (a) One
 - (b) Two
 - (c) Three
 - (d) Five

- 12. How many geometric progressions is/are possible containing 27, 8 and 12 as three of its/their terms?
 - (a) One
 - (b) Two
 - (c) Four
 - (d) Infinitely many
- 13. Let R be a relation from A = {1, 2, 3, 4} to B = {1, 3, 5} such that R = {(a, b) : a < b, where a ∈ A and b ∈ B}.</p>
 What is RoR⁻¹ equal to?
 - (a) {(1, 3), (1, 5), (2, 3), (2, 5), (3, 5), (4, 5)}
 - (b) {(3, 1), (5, 1), (3, 2), (5, 2), (5, 3), (5, 4)}
 - (c) {(3, 3), (3, 5), (5, 3), (5, 5)}
 - (d) {(3, 3), (3, 4), (4, 5)}
- 14. A five-digit number divisible by 3 is to be formed using the digits 0, 1, 2, 3 and 4 without repetition of digits. What is the number of ways this can be done?
 - (a) 96
 - (b) 48
 - (c) 32
 - (d) No number can be formed
- 15. What is ${}^{47}C_4 + {}^{51}C_3 + \sum_{j=2}^{5} {}^{52-j}C_3$ equal to ?
 - (a) 52C4
 - (b) 51C₅
 - (e) 53C₄
 - (d) 52C5

Consider the following for the next three (03) items that follow:

Let a, x, y, z, b be in AP, where x + y + z = 15. Let a, p, q, r, b be in HP, where $p^{-1} + q^{-1} + r^{-1} = 5/3$.

- 16. What is the value of ab?
 - (a) 10
 - (b) 9
 - (c) 8
 - (d) 6
- 17. What is the value of xyz?
 - (a) 120
 - (b) 105
 - (c) 90
 - (d) Cannot be determined
- 18. What is the value of pqr?
 - (a) 35/243
 - (b) 81/35
 - (c) 243/35
 - (d) Cannot be determined

Consider the following for the next two (02) items that follow:

The sixth term of an AP is 2 and its common difference is greater than 1.

- 19. What is the common difference of the AP so that the product of the first, fourth and fifth terms is greatest?
 - (a) 8/5
 - (b) 9/5
 - (c) 2
 - (d) 11/5
- 20. What is the first term of the AP so that the product of the first, fourth and fifth terms is greatest?
 - (a) -4
 - (b) -6
 - (c) -8
 - (d) -10

Consider the following for the next two (02) items that follow:

Let
$$ax^3 + bx^2 + cx + d = \begin{vmatrix} x+1 & 2x & 3x \\ 2x+3 & x+1 & x \\ 2-x & 3x+4 & 5x-1 \end{vmatrix}$$

then

- 21. What is the value of c?
 - (a) -1
 - (b) 34
 - (e) 35
 - (d) 50
- 22. What is the value of a + b + c + d?
 - (a) 62
 - (b) 63
 - (c) 65
 - (d) 68

Consider the following for the next two (02) items that follow:

The interior angles of a polygon of n sides are in AP.

The smallest angle is 120° and the common difference is 5°.

- 23. How many possible values can n have?
 - (a) One
 - (b) Two
 - (c) Three
 - (d) Infinitely many
- 24. What is the largest interior angle of the polygon?
 - (a) 160° only
 - (b) 195° only
 - (c) Either 160° or 195°
 - (d) Neither 160° nor 195°

25. If
$$m = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$
 and $n = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$, then what $\begin{bmatrix} 28 \end{bmatrix}$. If $A = \begin{bmatrix} 1 & -1 \\ 2 & 3 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 3 \\ -1 & -2 \end{bmatrix}$, then

is the value of the determinant of

 $m \cos \theta - n \sin \theta$?

- (a) -1
- (b) 0
- (c) 1
- (d) 2

26. If
$$f(x) = \begin{bmatrix} \cos x & -\sin x & 0 \\ \sin x & \cos x & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
, then which of

the following are correct?

- 1. $f(\theta) \times f(\phi) = f(\theta + \phi)$.
- 2. The value of the determinant of the matrix $f(\theta) \times f(\phi)$ is 1.
- 3. The determinant of f(x) is an even function.

Select the correct answer using the code given below:

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- 1, 2 and 3 (d)
- Which of the following are correct in respect 27. of the system of equations x + y + z = 8, x - y + 2z = 6 and 3x - y + 5z = k?
 - 1. They have no solution, if k = 15.
 - 2. They have infinitely many solutions, if 30. k = 20.
 - They have unique solution, if k = 25. 3.

Select the correct answer using the code given below:

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

28. If
$$A = \begin{bmatrix} 1 & -1 \\ 2 & 3 \end{bmatrix}$$
 and $B = \begin{bmatrix} 2 & 3 \\ -1 & -2 \end{bmatrix}$, then

which of the following is/are correct?

- AB (A-1 B-1) is a unit matrix. 100
- $(AB)^{-1} = A^{-1}B^{-1}$

Select the correct answer using the code given below:

- 1 only (a)
- (b) 2 only
- Both 1 and 2 (c)
- Neither 1 nor 2 (d)
- If $x^{ln\left(\frac{y}{z}\right)}$, $y^{ln(xz)^2}$, $z^{ln\left(\frac{x}{y}\right)} = y^{4 ln y}$ for any x > 1, y > 1 and z > 1, then which one of the following is correct?
 - In y is the GM of ln x, ln x, ln x and ln z (a)
 - (b) In y is the AM of ln x, ln x, ln x and ln z
 - In y is the HM of ln x, ln x, ln x and ln z (c)
 - (d) In y is the AM of ln x, ln x, ln z and ln z
- If the number 235 in decimal system is converted into binary system, then what is the resulting number?
 - (a) $(111110011)_2$
 - (b) (111010111)
 - (c) $(11110101)_{\alpha}$
 - (d) $(11011011)_{9}$

Consider the following for the next two (02) 34. items that follow:

Let α and β be the roots of the equation

$$x^{2} - (1 - 2a^{2}) x + (1 - 2a^{2}) = 0,$$

- 31. Under what condition does the above equation have real roots?
 - (a) $a^2 < \frac{1}{2}$
 - (b) $a^2 > \frac{1}{2}$
 - $(e) \quad a^2 \leq \frac{1}{2}$
 - (d) $a^2 \ge \frac{1}{2}$
- 32. Under what condition is $\frac{1}{\alpha^2} + \frac{1}{\beta^2} < 1$?
 - (a) $a^2 < \frac{1}{2}$
 - (b) $a^2 > \frac{1}{2}$
 - (c) a² > 1
 - (d) $a^2 \in \left(\frac{1}{3}, \frac{1}{2}\right)$ only
- 33. What is $\sqrt{\frac{1+\omega^2}{1+\omega}}$ equal to, where ω is the cube root of unity?
 - (a) 1
 - (b) ω
 - (c) ω²
 - (d) $i\omega$, where $i = \sqrt{-1}$

- 34. In an examination, 70% students passed in Physics, 80% students passed in Chemistry, 75% students passed in Mathematics and 85% students passed in Biology, and x% students failed in all the four subjects. What is the minimum value of x?
 - (a) 10
 - (b) 12
 - (c) 15
 - (d) None of the above

Consider the following for the next two (02) items that follow:

For the system of linear equations 2x + 3y + 5z = 9, 7x + 3y - 2z = 8 and $2x + 3y + \lambda z = \mu$

- 35. Under what condition does the above system of equations have infinitely many solutions?
 - (a) $\lambda = 5$ and $\mu \neq 9$
 - (b) $\lambda = 5$ and $\mu = 9$
 - (c) $\lambda = 9$ and $\mu = 5$
 - (d) $\lambda = 9$ and $\mu \neq 5$
- 36. Under what condition does the above system of equations have unique solutions?
 - (a) $\lambda = 5$ and $\mu = 9$
 - (b) $\lambda \neq 5$ and $\mu = 7$ only
 - (c) $\lambda \neq 5$ and μ has any real value
 - (d) λ has any real value and $\mu \neq 9$
- 37. What is the number of odd integers between 1000 and 9999 with no digit repeated?
 - (a) 2100
 - (b) 2120
 - (c) 2240
 - (d) 3331

38. What is the greatest value of the positive integer n satisfying the condition

$$1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots + \frac{1}{2^{n-1}} < 2 - \frac{1}{1000}$$
?

- (a) 8
- (b) 9
- (c) 10
- (d) 11

Consider the following for the next two (02) items that follow:

 $2x^2 + 3x - \alpha = 0$ has roots -2 and β while the equation $x^2 - 3mx + 2m^2 = 0$ has both roots positive, where $\alpha > 0$ and $\beta > 0$.

- 39. What is the value of α ?
 - (a) 1/2
 - (b) 1
 - (c) 2
 - (d) 4
- 40. If β, 2, 2m are in GP, then what is the value of β√m?
 - (a) 1
 - (b) 2
 - (c) 4
 - (d) 6
- 41. sin A + 2 sin 2A + sin 3A is equal to which of the following?
 - $1. \qquad 4 \sin 2A \cos^2 \left(\frac{A}{2}\right)$
 - 2. $2 \sin 2A \left(\sin \frac{A}{2} + \cos \frac{A}{2} \right)^2$
 - 3. $8 \sin A \cos A \cos^2 \left(\frac{A}{2}\right)$

Select the correct answer using the code given below:

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

- the 42. If $x = \sin 70^\circ$. $\sin 50^\circ$ and $y = \cos 60^\circ$. $\cos 80^\circ$, then what is xy equal to?
 - (a) 1/16
 - (b) 1/8
 - (c) 1/4
 - (d) 1/2
 - 43. If $\sin \theta_1 + \sin \theta_2 + \sin \theta_3 + \sin \theta_4 = 4$, then what is the value of $\cos \theta_1 + \cos \theta_2 + \cos \theta_3 + \cos \theta_4$?
 - (a) 0
 - (b) 1
 - (c) 2
 - (d) 4
 - 44. What is the value of

$$\left(1+\cos\frac{\pi}{8}\right)\left(1+\cos\frac{3\pi}{8}\right)\left(1+\cos\frac{5\pi}{8}\right)\left(1+\cos\frac{7\pi}{8}\right)?$$

- (a) $\frac{1}{2}$
- (b) $\frac{1}{2} + \frac{1}{2\sqrt{2}}$
- (c) $\frac{1}{2} \frac{1}{2\sqrt{2}}$
- (d) 1/8
- 45. If $x \cos \theta + y \sin \theta = z$, then what is the value of $(x \sin \theta y \cos \theta)^2$?
 - (a) $x^2 + y^2 z^2$
 - (b) $x^2 y^2 z^2$
 - (c) $x^2 y^2 + z^2$
 - (d) $x^2 + y^2 + z^2$

- 46. What is the value of cos (2 cos-1 0.8)?
 - (a) 0.81
 - (b) 0.56
 - (c) 0.48
 - (d) 0.28
- 47. The top of a hill when observed from the top and bottom of a building of height h is at angles of elevation p and q respectively. What is the height of the hill?
 - (a) $\frac{h \cot q}{\cot q \cot p}$
 - (b) $\frac{h \cot p}{\cot p \cot q}$
 - (c) $\frac{2h \tan p}{\tan p \tan q}$
 - $(d) = \frac{2h \tan q}{\tan q \tan p}$
- 48. If $\sin 18^\circ = \frac{\sqrt{5} 1}{4}$, then what is the value of $\sin 81^\circ$?
 - (a) $\frac{\sqrt{3+\sqrt{5}}+\sqrt{5-\sqrt{5}}}{4}$
 - (b) $\frac{\sqrt{3+\sqrt{5}}+\sqrt{5+\sqrt{5}}}{4}$
 - (c) $\frac{\sqrt{3-\sqrt{5}}+\sqrt{5-\sqrt{5}}}{4}$
 - (d) $\frac{\sqrt{3+\sqrt{5}}-\sqrt{5-\sqrt{5}}}{4}$

- 49. A moving boat is observed from the top of a cliff of 150 m height. The angle of depression of the boat changes from 60° to 45° in 2 minutes. What is the speed of the boat in metres per hour?
 - (a) $\frac{4500}{\sqrt{3}}$
 - (b) $\frac{4500(\sqrt{3}-1)}{\sqrt{3}}$
 - (c) 4500√3
 - (d) $\frac{4500(\sqrt{3}+1)}{\sqrt{3}}$
- 50. What is $\frac{1 \tan 2^{\circ} \cot 62^{\circ}}{\tan 152^{\circ} \cot 88^{\circ}}$ equal to ?
 - (a) √3
 - (b) -√3
 - (c) $\sqrt{2} 1$
 - (d) 1 √2
- 51. An equilateral triangle has one vertex at (0, 0) and another at (3, √3). What are the coordinates of the third vertex?
 - (a) $(0, 2\sqrt{3})$ only
 - (b) $(3, -\sqrt{3})$ only
 - (c) $(0, 2\sqrt{3})$ or $(3, -\sqrt{3})$
 - (d) Neither $(0, 2\sqrt{3})$ nor $(3, -\sqrt{3})$
- 52. What is the equation of the right bisector of the line segment joining (1, 1) and (2, 3)?
 - (a) 2x + 4y 11 = 0
 - (b) 2x 4y 5 = 0
 - (c) 2x 4y 11 = 0
 - (d) x y + 1 = 0

- 53. What is the radius of the circle passing 57. through the point (2, 4) and having centre at the intersection of the lines x y = 4 and 2x + 3y + 7 = 0?
 - (a) 3 units
 - (b) 5 units
 - (c) 3√3 units
 - (d) $5\sqrt{2}$ units
- 54. What is the equation of the hyperbola having latus rectum and eccentricity 8 and $\frac{3}{\sqrt{5}}$ respectively?
 - (a) $\frac{x^2}{25} \frac{y^2}{20} = 1$
 - (b) $\frac{x^2}{40} \frac{y^2}{20} = 1$
 - (c) $\frac{x^2}{40} \frac{y^2}{30} = 1$
 - (d) $\frac{x^2}{30} \frac{y^2}{25} = 1$
- 55. If the point (a, a) lies between the lines | x + y | = 2, then which one of the following is correct?
 - (a) | a | < 2
 - (b) | a | < √2
 - (c) | a | < 1
 - (d) | a | $<\frac{1}{\sqrt{2}}$
- 56. What is the equation of the straight line which passes through the point of intersection of the straight lines x + 2y = 5 and 3x + 7y = 17 and is perpendicular to the straight line 3x + 4y = 10?
 - (a) 4x + 3y + 2 = 0
 - (b) 4x y + 2 = 0
 - (c) 4x 3y 2 = 0
 - (d) 4x 3y + 2 = 0

- 57. If (a, b) is at unit distance from the line 8x + 6y + 1 = 0, then which of the following conditions are correct?
 - 1. 3a 4b 4 = 0
 - 2. 8a + 6b + 11 = 0
 - 3. 8a + 6b 9 = 0

Select the correct answer using the code given below:

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3
- 58. If the ellipse 9x² + 16y² = 144 intercepts the line 3x + 4y = 12, then what is the length of the chord so formed?
 - (a) 5 units
 - (b) 6 units
 - (c) 8 units
 - (d) 10 units
- 59. A straight line cuts off an intercept of 2 units on the positive direction of x-axis and passes through the point (-3, 5). What is the foot of the perpendicular drawn from the point (3, 3) on this line?
 - (a) (1, 3)
 - (b) (2,0)
 - (c) (0, 2)
 - (d) (1, 1)
- 60. What is the eccentricity of rectangular hyperbola?
 - (a) √2
 - (b) √3
 - (c) √5
 - (d) √6

Consider the following for the next two (02) 64. items that follow:

Let Q be the image of the point P(-2, 1, -5) in the plane 3x - 2y + 2z + 1 = 0.

61. Consider the following:

- 1. The coordinates of Q are (4, -3, -1).
- 2. PQ is of length more than 8 units.
- The point (1, -1, -3) is the mid-point of the line segment PQ and lies on the given plane.

Which of the above statements are correct?

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

62. Consider the following:

- The direction ratios of the line segment PQ are < 3, -2, 2 >.
- The sum of the squares of direction cosines of the line segment PQ is unity.

Which of the above statements is/are correct?

- (a) 1 only
- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2

Consider the following for the next two (02) items that follow:

A line L passes through the point P(5, -6, 7) and is parallel to the planes x + y + z = 1 and 2x - y - 2z = 3.

- 63. What are the direction ratios of the line of intersection of the given planes?
 - (a) < 1, 4, 3 >
 - (b) <-1,-4,3>
 - (c) < 1, -4, 3 >
 - (d) <1,-4,-3>

- 64. What is the equation of the line L?
 - (a) $\frac{x-5}{-1} = \frac{y+6}{4} = \frac{z-7}{-3}$
 - (b) $\frac{x+5}{-1} = \frac{y-6}{4} = \frac{z+7}{-3}$
 - (c) $\frac{x-5}{-1} = \frac{y+6}{-4} = \frac{z-7}{3}$
 - (d) $\frac{x-5}{-1} = \frac{y+6}{-4} = \frac{z-7}{-3}$

Consider the following for the next two (02) items that follow:

Let $\overrightarrow{a} = \hat{i} + \hat{j}$, $\overrightarrow{b} = 3\hat{i} + 4\hat{k}$ and $\overrightarrow{b} = \overrightarrow{c} + \overrightarrow{d}$, where \overrightarrow{c} is parallel to \overrightarrow{a} and \overrightarrow{d} is perpendicular to \overrightarrow{a} .

- 65. What is c equal to?
 - (a) $\frac{3(\hat{i}+\hat{j})}{2}$
 - (b) $\frac{2(\hat{i} + \hat{j})}{3}$
 - $(c) \qquad \frac{(\hat{i}+\hat{j})}{2}$
 - (d) $\frac{(\hat{i} + \hat{j})}{3}$
- 66. If $\overrightarrow{d} = x \hat{i} + y \hat{j} + z \hat{k}$, then which of the following equations is/are correct?
 - 1. y x = 4
 - 2. 2z 3 = 0

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2

Consider the following for the next two (02) 72. items that follow:

Let \overrightarrow{a} , \overrightarrow{b} and \overrightarrow{c} be three vectors such that \overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} = $\overrightarrow{0}$, and $|\overrightarrow{a}|$ = 10, $|\overrightarrow{b}|$ = 6 and $|\overrightarrow{c}|$ = 14.

- 67. What is \overrightarrow{a} . \overrightarrow{b} + \overrightarrow{b} . \overrightarrow{c} + \overrightarrow{c} . \overrightarrow{a} equal to?
 - (a) -332
 - (b) -166
 - (c) 0
 - (d) 166
- **68.** What is the angle between \overrightarrow{a} and \overrightarrow{b} ?
 - (a) 30°
 - (b) 45°
 - (c) 60°
 - (d) 75°
- 69. In a right-angled triangle ABC, if the hypotenuse AB = p, then what is

$$\overrightarrow{AB}$$
. \overrightarrow{AC} + \overrightarrow{BC} . \overrightarrow{BA} + \overrightarrow{CA} . \overrightarrow{CB} equal to ?

- (a) p
- (b) p²
- (c) 2p2
- $(d) \quad \frac{p^2}{2}$
- 70. A force $\overrightarrow{F} = 3\hat{i} + 2\hat{j} 4\hat{k}$ is applied at the point (1, -1, 2). What is the moment of the force about the point (2, -1, 3)?
 - (a) $\hat{i} + 4\hat{j} + 4\hat{k}$
 - (b) $2\hat{i} + \hat{j} + 2\hat{k}$
 - (c) 2î-7ĵ-2k
 - (d) 2î + 4ĵ k
- 71. What is the domain of the function $f(x) = \frac{1}{\sqrt{|x| x}}$?
 - (a) (- ∞, 0)
 - (b) (0, ∞)
 - (c) 0 < x < 1
 - (d) x>1

- 72. Consider the following in respect of the function $f(x) = \begin{cases} 2 + x, & x \ge 0 \\ 2 x, & x < 0 \end{cases}$
 - 1. $\lim_{x \to 1} f(x)$ does not exist.
 - 2. f(x) is differentiable at x = 0.
 - 3. f(x) is continuous at x = 0.

Which of the above statements is/are correct?

- (a) 1 only
- (b) 3 only
- (c) 2 and 3 only
- (d) 1 and 3 only
- 73. Let f: A → R where A = R \((0)) is such that
 f(x) = x + |x| \(x \). On which one of the following sets is f(x) continuous?
 - (a) A
 - (b) $B = \{x \in \mathbb{R} : x \ge 0\}$
 - (c) $C = \{x \in \mathbb{R} : x \le 0\}$
 - (d) D = R
- 74. Which one of the following statements is correct in respect of the function f(x) = x³ sin x?
 - (a) It has local maximum at x = 0.
 - (b) It has local minimum at x = 0.
 - (c) It has neither maximum nor minimum at x = 0.
 - (d) It has maximum value 1.
- 75. What is the area bounded by the curves

$$|y| = 1 - x^2$$
?

- (a) 4/3 square units
- (b) 8/3 square units
- (c) 4 square units
- (d) 16/3 square units

Consider the following function for the next 80. two (02) items that follow:

$$f(x) = \begin{cases} 3x^2 + 12x - 1, & -1 \le x \le 2 \\ 37 - x, & 2 < x \le 3 \end{cases}$$

- 76. Which of the following statements is/are correct?
 - 1. f(x) is increasing in the interval [-1, 2].
 - 2. f(x) is decreasing in the interval (2, 3].

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2
- 77. Which of the following statements are correct?
 - 1. f(x) is continuous at x = 2.
 - f(x) attains greatest value at x = 2.
 - f(x) is differentiable at x = 2.

Select the correct answer using the code given below:

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

Consider the following for the next three (03) items that follow:

Let
$$f(x) = (|x| - |x - 1|)^2$$
.

- 78. What is f'(x) equal to when x > 1?
 - (a) 0
 - (b) 2x 1
 - (c) 4x 2
 - (d) 8x 4
- 79. What is f'(x) equal to when 0 < x < 1?
 - (a) 0
 - (b) 2x 1
 - (c) 4x 2
 - (d) 8x 4

- 80. Which of the following equations is/are correct?
 - 1. f(-2) = f(5)
 - 2. f''(-2) + f''(0.5) + f''(3) = 4

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2

Consider the following for the next three (03) items that follow:

Let f(x) = [x], where [.] is the greatest integer function and $g(x) = \sin x$ be two real valued functions over \mathbb{R} .

- 81. Which of the following statements is correct?
 - (a) Both f(x) and g(x) are continuous at x = 0.
 - (b) f(x) is continuous at x = 0, but g(x) is not continuous at x = 0.
 - (c) g(x) is continuous at x = 0, but f(x) is not continuous at x = 0,
 - (d) Both f(x) and g(x) are discontinuous at x = 0.
- 82. Which one of the following statements is correct?
 - (a) $\lim_{x\to 0} (fog)(x)$ exists.
 - (b) $\lim_{x\to 0} (gof)(x)$ exists.
 - (c) $\lim_{x\to 0^-} (f \circ g)(x) = \lim_{x\to 0^-} (g \circ f)(x)$
 - (d) $\lim_{x\to 0+} (f \circ g)(x) = \lim_{x\to 0+} (g \circ f)(x)$
- 83. Which of the following statements are correct?
 - 1. (fof)(x) = f(x).
 - 2. $(g \circ g)(x) = g(x)$ only when x = 0.
 - (go(fog)) (x) can take only three values.
 Select the correct answer using the code given below:
 - (a) 1 and 2 only
 - (b) 2 and 3 only
 - (c) 1 and 3 only
 - (d) 1, 2 and 3

Consider the following for the next two (02) items that follow:

Let $f(x) = \begin{cases} \frac{e^x - 1}{x}, & x > 0 \\ 0, & x = 0 \end{cases}$ be a real valued function.

- 84. Which one of the following statements is correct?
 - (a) f(x) is a strictly decreasing function in 88.(0, x).
 - (b) f(x) is a strictly increasing function in (0, x).
 - f(x) is neither increasing nor decreasing in (0, x).
 - (d) f(x) is not decreasing in (0, x).
- 85. Which of the following statements is/are correct?
 - 1. f(x) is right continuous at x = 0.
 - 2. f(x) is discontinuous at x = 1.

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2

Consider the following for the next two (02) items that follow:

Consider the parabola $y = x^2 + 7x + 2$ and the straight line y = 3x - 3.

- 86. What are the coordinates of the point on the parabola which is closest to the straight line?
 - (a) (0, 2)
 - (b) (-2, -8)
 - (c) (-7, 2)
 - (d) (1, 10)
- 87. What is the shortest distance from the above point on the parabola to the line?
 - (a) $\frac{\sqrt{10}}{2}$
 - (b) $\frac{\sqrt{10}}{5}$
 - (c) $\frac{1}{\sqrt{10}}$
 - (d) $\frac{\sqrt{5}}{4}$

Consider the following for the next three (03) items that follow:

Let
$$f(x) =$$

$$\begin{cases}
-2, & -3 \le x \le 0 \\
x - 2, & 0 < x \le 3
\end{cases}$$
 and
$$g(x) = f(|x|) + |f(x)|$$

- 88. Which of the following statements is/are correct?
 - 1. g(x) is differentiable at x = 0.
 - 2. g(x) is differentiable at x = 2.

Select the correct answer using the code given below:

- (a) 1 only
- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2
- 89. What is the value of the differential coefficient of g(x) at x = -2?
 - (a) -1
 - (b) 0
 - (c) 1
 - (d) 2
- 90. Which of the following statements are correct?
 - 1. g(x) is continuous at x = 0.
 - 2. g(x) is continuous at x = 2.
 - 3. g(x) is continuous at x = -1.

Select the correct answer using the code given below:

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

91. Let f(x) be a function such that

$$f'\left(\frac{1}{x}\right) + x^3 f'(x) = 0$$
. What is $\int_{-1}^{1} f(x) dx$

equal to?

- (a) 2 f(1)
- (b) 0
- (c) 2 f(-1)
- (d) 4 f(1)

92. What is $\int \frac{x^4 - 1}{x^2 \sqrt{x^4 + x^2 + 1}} dx$ equal to?

$$(a) \qquad \sqrt{\frac{x^4+x^2+1}{x}}+c$$

(b)
$$\sqrt{x^4 + 2 - \frac{1}{x^2}} + c$$

(c)
$$\sqrt{x^2 + \frac{1}{x^2} + 1} + c$$

(d)
$$\sqrt{\frac{x^4 - x^2 + 1}{x}} + c$$

93. What are the degree and order respectively of the differential equation satisfying $e^{y\sqrt{1-x^2}+x\sqrt{1-y^2}}=ce^x, \ (\text{where } c>0, \ |x|<1, \ |y|<1)\ ?$

- (a) 1, 1
- (b) 1, 2
- (c) 2, 1
- (d) 2, 2

94. What is the curve which passes through the point (1, 1) and whose slope is $\frac{2y}{x}$?

- (a) Circle
- (b) Parabola
- (c) Ellipse
- (d) Hyperbola

95. If $x dy = y dx + y^2 dy$, y > 0 and y(1) = 1, then what is y(-3) equal to ?

- (a) 3 only
- (b) -1 only
- (c) Both -1 and 3
- (d) Neither -1 nor 3

96. What is the order of the differential equation

$$\frac{dx}{dy} + \int y \, dx = x^3 \ ?$$

- (a) 1
- (b) 2
- (e) 3
- (d) Cannot be determined

97. Which one of the following differential equations represents the family of straight lines which are at unit distance from the origin?

(a)
$$\left(y - x \frac{dy}{dx}\right)^2 = 1 - \left(\frac{dy}{dx}\right)^2$$

(b)
$$\left(y + x \frac{dy}{dx}\right)^2 = 1 + \left(\frac{dy}{dx}\right)^2$$

(c)
$$\left(y - x \frac{dy}{dx}\right)^2 = 1 + \left(\frac{dy}{dx}\right)^2$$

(d)
$$\left(y + x \frac{dy}{dx}\right)^2 = 1 - \left(\frac{dy}{dx}\right)^2$$

98. What is $\int e^{\sin x} \frac{x \cos^3 x - \sin x}{\cos^2 x} dx \text{ equal to ?}$

- (a) $(x + \sec x) e^{\sin x} + c$
- (b) $(x \sec x) e^{\sin x} + c$
- (c) $(x + \tan x) e^{\sin x} + c$
- (d) $(x \tan x) e^{\sin x} + c$

99. If
$$\int_{0}^{\pi/2} \frac{dx}{3\cos x + 5} = k \cot^{-1} 2$$
, then what is the

value of k?

- (a) 1/4
- (b) 1/2
- (c) 1
- (d) 2
- 100. What is $\int_{1}^{3} |1-x^4| dx$ equal to?
 - (a) -232/5
 - (b) -116/5
 - (c) 116/5
 - (d) 232/5
- 101. A special dice with numbers 1, -1, 2, -2, 0 and 3 is thrown thrice. What is the probability that the sum of the numbers occurring on the upper face is zero?
 - (a) 1/72
 - (b) 1/8
 - (c) 7/72
 - (d) 25/216
- 102. There is 25% chance that it rains on any particular day. What is the probability that there is at least one rainy day within a period of 7 days?
 - (a) $1 \left(\frac{1}{4}\right)^7$
 - (b) $\left(\frac{1}{4}\right)^7$
 - (e) $\left(\frac{3}{4}\right)^7$
 - (d) $1 \left(\frac{3}{4}\right)^7$

- 103. A salesman has a 70% chance to sell a product to any customer. The behaviour of successive customers is independent. If two customers A and B enter, what is the probability that the salesman will sell the product to customer A or B?
 - (a) 0.98
 - (b) 0.91
 - (c) 0.70
 - (d) 0·49
- 104. A student appears for tests I, II and III. The student is considered successful if he passes in tests I, II or I, III or all the three. The probabilities of the student passing in tests I, II and III are m, n and 1/2 respectively. If the probability of the student to be successful is 1/2, then which one of the following is correct?
 - (a) m(1+n)=1
 - (b) n (1+m) = 1
 - (c) m = 1
 - (d) mn = 1
- 105. Three candidates solve a question. Odds in favour of the correct answer are 5: 2, 4: 3 and 3: 4 respectively for the three candidates. What is the probability that at least two of them solve the question correctly?
 - (a) 209/343
 - (b) 134/343
 - (c) 149/343
 - (d) 60/343

- 106. Consider the following statements:
 - The mean and median are equal in symmetric distribution.
 - The range is the difference between the maximum value and the minimum value in the data.
 - The sum of the areas of the rectangles in the histogram is equal to the total area bounded by the frequency polygon and the horizontal axis.

Which of the above statements are correct?

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3
- 107. The scores of 15 students in an examination were recorded as 10, 5, 8, 16, 18, 20, 8, 10, 16, 20, 18, 11, 16, 14 and 12. After calculating the mean, median and mode, an error is found. One of the values is wrongly written as 16 instead of 18. Which of the following measures of central tendency will change?
 - (a) Mean and median
 - (b) Median and mode
 - (c) Mode only
 - (d) Mean and mode
- 108. For 10 observations on price (x) and supply (y), the following data was obtained:

$$\sum x = 130$$
, $\sum y = 220$, $\sum x^2 = 2288$, $\sum y^2 = 5506$ and $\sum xy = 3467$.

What is the line of regression of y on x?

- (a) y = 0.91x + 8.74
- (b) y = 1.02x + 8.74
- (c) y = 1.02x 7.02
- (d) y = 0.91x 7.02

109. In a study of two groups, the following results were obtained:

	Group A	Group B
Sample size	20	25
Sample mean	22	23
Sample standard deviation	10	12

Which of the following statements is correct?

- (a) Group A is less variable than Group B because Group A's standard deviation is smaller.
- (b) Group A is less variable than Group B because Group A's sample size is smaller.
- (c) Group A is less variable than Group B because Group A's sample mean is smaller.
- (d) Group A is less variable than Group B because Group A's coefficient of variation is smaller.
- 110. Consider the following statements in respect of class intervals of grouped frequency distribution:
 - Class intervals need not be mutually exclusive.
 - 2. Class intervals should be exhaustive.
 - Class intervals need not be of equal width.

Which of the above statements are correct?

- (a) 1 and 2 only
- (b) 2 and 3 only
- (c) 1 and 3 only
- (d) 1, 2 and 3

- cure a patient. If the medicine is given to 5 patients, what is the probability that at least one patient is cured by this medicine?
 - (a) 1024
 - 243 (b) 1024
 - 1023 (c) 1024
 - 781 (d)
- 112. For two events, A and B, it is given that $P(A) = \frac{3}{5}$, $P(B) = \frac{3}{10}$ and $P(A | B) = \frac{2}{3}$. If \overline{A} and B are the complementary events of A and B, then what is P(A | B) equal to?
 - (a)
 - (b)
 - (c)
 - (d)
- A machine has three parts, A, B and C, whose chances of being defective are 0.02, 0.10 and 0.05 respectively. The machine stops working if any one of the parts becomes defective. What is the probability that the machine will not stop working?
 - (a) 0.06
 - (b) 0.16
 - (c) 0.84
 - (d) 0.94

111. A medicine is known to be 75% effective to 114. Three independent events, A1, A2 and A3 probabilities $P(A_i) = \frac{1}{1+i}$ with occur

> i = 1, 2, 3. What is the probability that at least one of the three events occurs?

- (a)
- (b)
- (c)
- (d)
- 115. Two variates, x and y, are uncorrelated and have standard deviations σ_x and σ_y What is the correlation respectively. coefficient between x + y and x - y?

 - (b) $\frac{\sigma_x + \sigma_y}{2\sigma_x\sigma_y}$
 - (c) $\frac{\sigma_x^2 \sigma_y^2}{\sigma_x^2 + \sigma_y^2}$
 - (d) $\frac{\sigma_y \sigma_x}{\sigma_x \sigma_y}$
- 116. A random sample of 20 people is classified in the following table according to their ages :

Age	Frequency
15 - 25	2
25 – 35	4
35 - 45	6
45 – 55	5
55 - 65	3

What is the mean age of this group of people?

- (a) 41.0
- 41.5 (b)
- 42.0 (c)
- (d) 42.5

- 117. If the covariance between x and y is 30, 119. In a series of 3 one-day cricket matches variance of x is 25 and variance of y is 144, between teams A and B of a college, the then what is the correlation coefficient?
 - (a) 0.4
 - (b) 0-5
 - (c) 0-6
 - (d) 0.7
- 118. A coin is tossed three times. Consider the following events:

A: No head appears

B: Exactly one head appears

C: At least two heads appear

Which one of the following is correct?

- (a) $(A \cup B) \cap (A \cup C) = B \cup C$
- (b) $(A \cap B') \cup (A \cap C') = B' \cup C'$
- (e) $A \cap (B' \cup C') = A \cup B \cup C$
- (d) $A \cap (B' \cup C') = B' \cap C'$

- 119. In a series of 3 one-day cricket matches between teams A and B of a college, the probability of team A winning or drawing are 1/3 and 1/6 respectively. If a win, loss or draw gives 2, 0 and 1 point respectively, then what is the probability that team A will score 5 points in the series?
 - (a) $\frac{17}{18}$
 - (b) $\frac{11}{12}$
 - (c) $\frac{1}{12}$
 - (d) $\frac{1}{18}$
- 120. Let the random variable X follow B(6, p). If 16 P(X = 4) = P(X = 2), then what is the value of p?
 - (a) $\frac{1}{3}$
 - (b) $\frac{1}{4}$
 - (c) $\frac{1}{5}$
 - (d) $\frac{1}{6}$